

1. (a) The energy of a particle is given by  $E(x) = ax^2$ , where  $a$  is a constant and  $x$  is a coordinate that takes value from 0 to  $\infty$ . Calculate the average energy per particle for a system of such particles obeying Maxwell-Boltzmann distribution law, at a temperature  $T$ . Does the result is in conformity with the law of equipartition of energy?
2. Make a rough plot (using Scilab) of the energy distribution at two different temperatures ( $T_1, T_2; T_1 > T_2$ ) for a system of free particles governed by (i) Maxwell-Boltzmann statistics
3. Partition function of monoatomic ideal gas given by  $Z = V \left( \frac{2\pi mk_B T}{h^2} \right)^{3/2}$  From this relation derive the ideal gas equation.
4. If the distribution function of  $x$  is  $f(x) = xe^{-x/\lambda}$  over the interval  $0 < x < \infty$ , the mean value of  $x$  is  
(a)  $\lambda$  (b)  $2\lambda$  (c)  $\frac{\lambda}{2}$  (D) 0
5. What is the probability that a deuce and ace appear when two dice are thrown?
6. Let  $N_{MB}$ ,  $N_{BE}$ , and  $N_{FD}$  denote the number of ways in which two particles can be distributed in two energy states according to Maxwell-Boltzmann, Bose-Einstein and Fermi-Dirac statistics respectively. Then find  $N_{MB} : N_{BE} : N_{FD}$ .
7. Plot Debye's relation for specific heat and  $C_v = \gamma T + \beta T^3$  on the same plot.  $\gamma$  and  $\beta$  is constant.